

# Approaches to Multidisciplinary Design Optimization

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### **Presentation Overview**

- What is multidisciplinary design optimization?
  - Why use it?
  - How is it used?
- Example MDO application
- Computational challenges in MDO
- Example surrogate modeling application



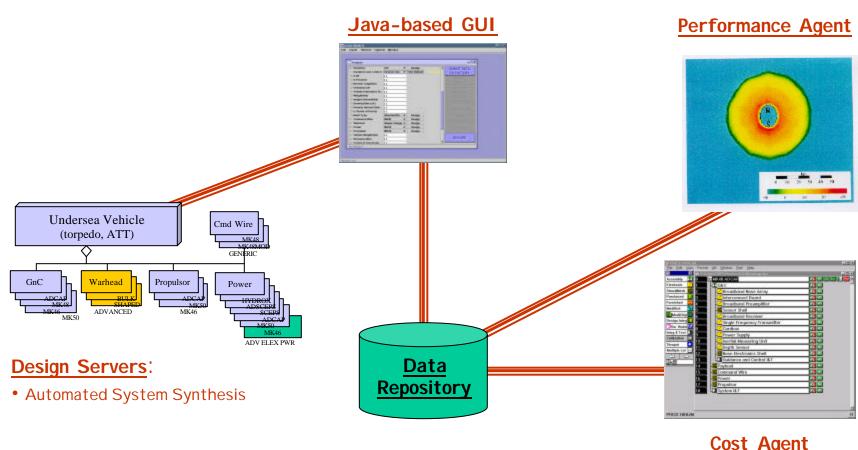
### What is MDO?

- Multidisciplinary design optimization (MDO):
  - is a methodology for the design of systems in which strong interactions between disciplines motivates designers to simultaneously manipulate variables in several disciplines
  - involves the coordination of multiple disciplinary analyses to realize more effective solutions during the design and optimization of complex systems



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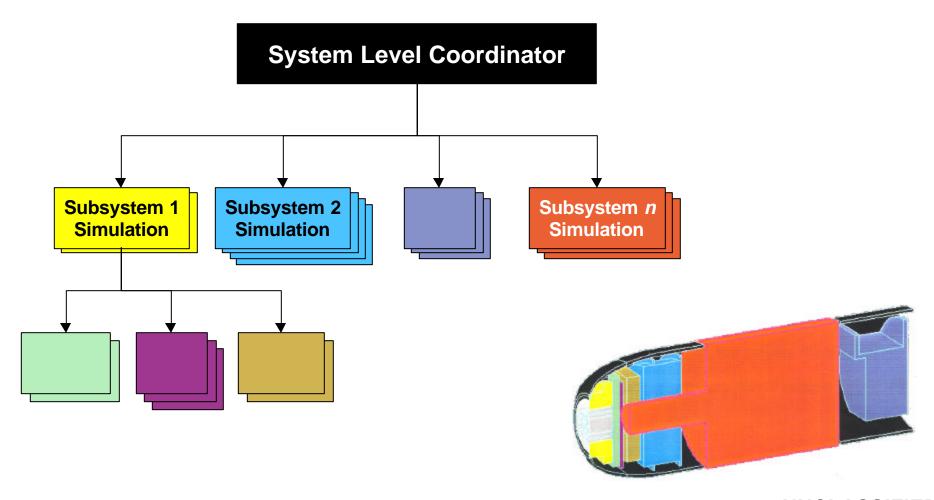
# Simulation-Based Design Architecture



**Cost Agent** 

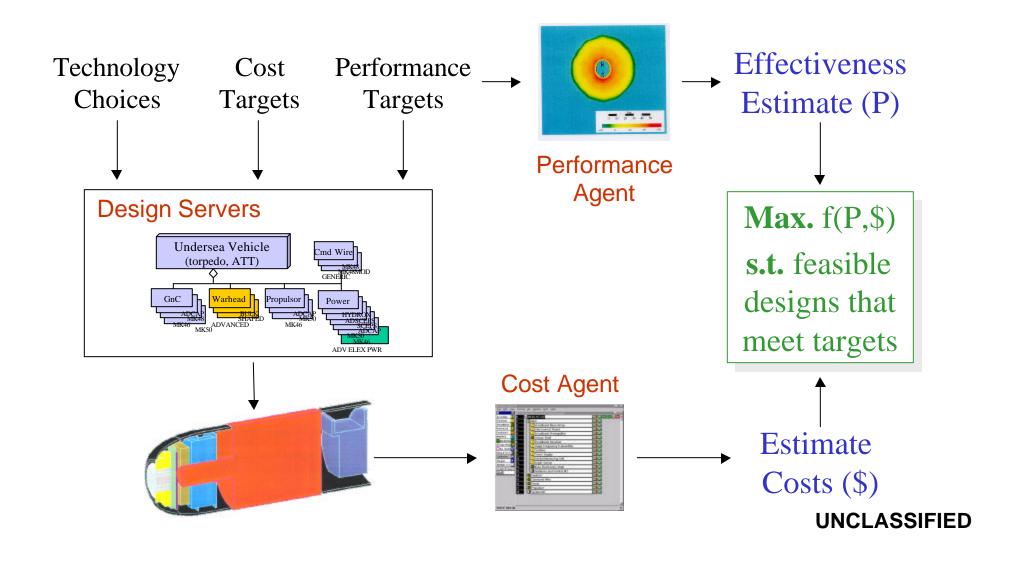


# **Design Server Interactions**





# **System-level Objective**







### How is it used?

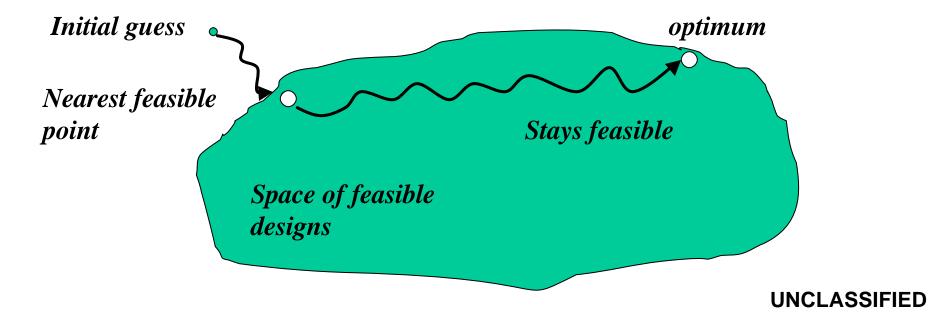
- Using MDO involves:
  - decomposing the system into multiple subsystems or disciplinary analyses
  - developing mathematically models and analyses for:
    - the "parent" system
    - each subsystem <u>and</u> its interactions
  - selecting an appropriate MDO formulation and algorithm
  - solving the MDO problem to generate solutions





# Multiple Discipline Feasible

- Get feasible and stay feasible
- Implies each iteration is a two part process:
  - move to improve design
  - re-establish feasibility

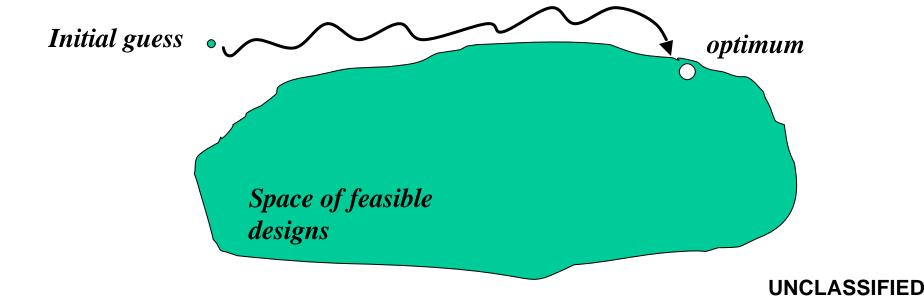






# **Individual Discipline Feasible**

- Go straight to optimum
- Since optimum usually on boundary, not feasible until optimal
  - equivalent to discrepancy = 0







# **Collaborative Optimization**

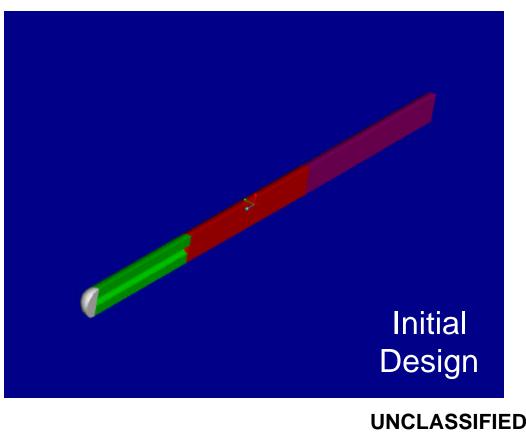
System-Level Optimizer Decompose Goal: Design objective s.t. Interdisciplinary system into compatibility constraints smaller units that can be Subspace Optimizer 1 Subspace Optimizer 2 Subspace Optimizer n individually Goal: Interdisciplinary Goal: Interdisciplinary Goal: Interdisciplinary compatibility compatibility compatibility optimized Analysis 1 Analysis 2 s.t. Analysis n s.t. s.t. and then constraints constraints constraints synthesized into a system Analysis 1 Analysis 2 Analysis n



# **Underwater Exploratory Vehicle**

- 4 Subsystems:
  - Guidance & Control
  - Instrumentation
  - Power
  - Propulsion
- Subsystem analyses developed by Erik Halberg (M.S., ME)

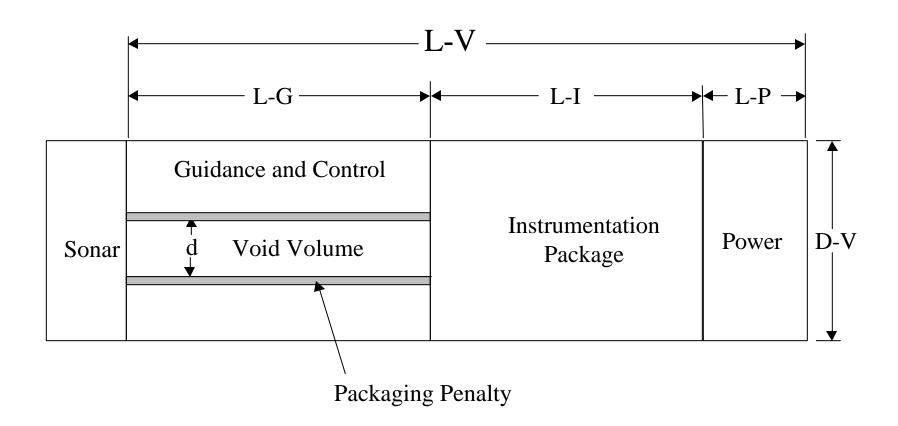
- 7 Design Variables:
  - Volumes







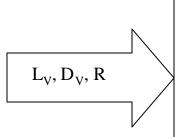
# **Underwater Vehicle Example**



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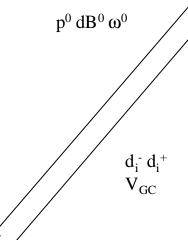
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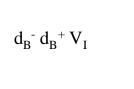


**Underwater Exploratory Vehicle** 

$$\begin{split} & Min \, P_1(d_8^-) + P_2(d_4^-) + P_3(d_5^- + d_6^- + d_7^-) + \\ & P_4(d_1^- + d_2^- + d_3^-) \\ & st \\ & L_{GC} + L_P + L_I - L_V = 0 \\ & (e^0 - d_E^- + d_E^+) * 50/(s^0 - d_S^- + d_S^+) - R = 0 \end{split}$$



 $pn^0$   $\int$   $e^0 hp^0 sp^0$ 



 $d_S^- d_S^+ SP$ 

#### Guidance & Control

Min 
$$\Sigma(d_i^- + d_i^+)$$
  $i = 1,2,3$   
st  
 $P(V) + d_3^- - d_3^+ = p^0$   
 $dB(V) + d_2^- - d_2^+ = dB^0$   
 $\omega(V) + d_1^- - d_1^+ = \omega^0$ 

Instrumentation

Min 
$$d_4^- + d_4^+$$
  
st  
Pn(V) +  $d_4^- - d_4^+ = pn^0$ 

Power

 $s^0$ 

 $d_i^- d_i^+ V_P$ 

Min 
$$\Sigma(d_k^- + d_k^+) k = 5,6,7$$
  
st  
 $E(V) + d_6^- - d_6^+ = e^0$   
 $HP(V) + d_7^- - d_7^+ = hp^0$   
 $SP(V) + d_5^- - d_5^+ = sp^0$ 

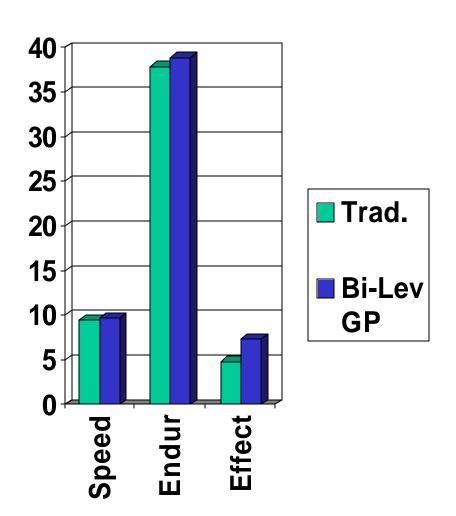
Propulsion

Min 
$$d_8^- + d_8^+$$
  
st  
S(SP) +  $d_8^- - d_8^+ = s^0$ 



### **Vehicle Performance**

- MDO formulation yields superior performance:
  - Speed
  - Endurance
  - Effectiveness

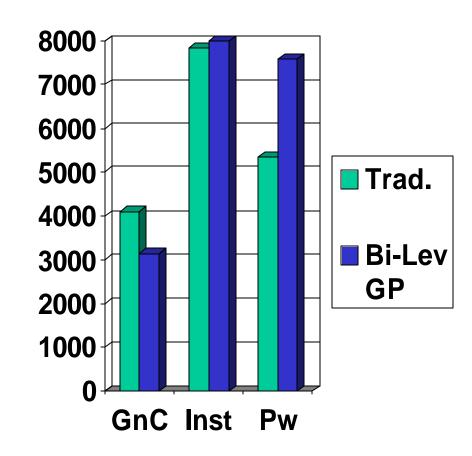




# **Vehicle Optimization**

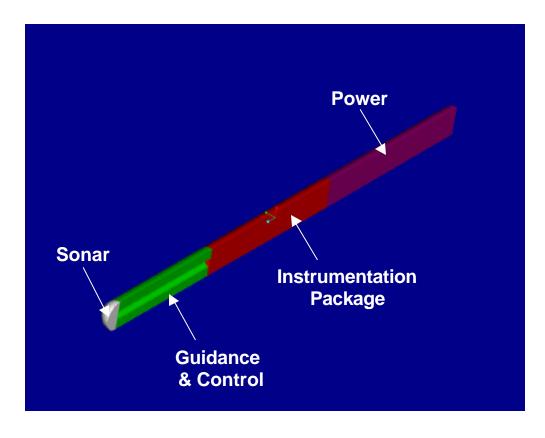
- Final Design:
  - Slightly different configurations

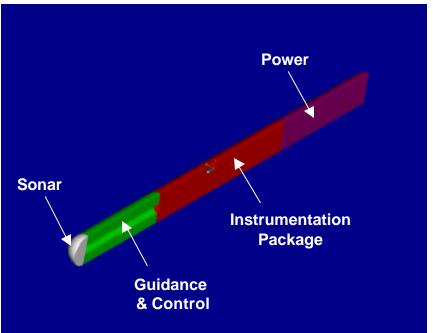
- Solution Time:
  - 1 minute vs. 3 hours

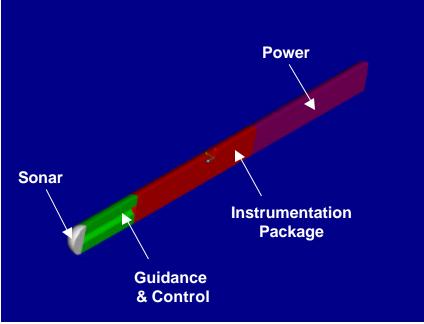




# **Vehicle Configurations**











# Computational Challenges in MDO

- In MDO, computer simulation codes are:
  - often "black-box" in nature
  - discipline-specific
  - composed in different languages (e.g., Fortran, C, Java)
  - distributed, both geographically and on different computer platforms
  - computationally expensive due to fidelity of modeling and need for accurate results



# **Surrogate Models for MDO**

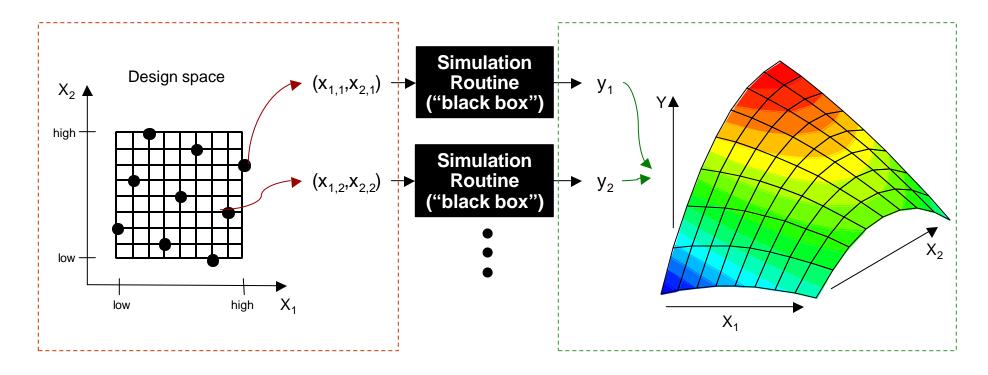
- Surrogate models are fast, simple approximations of computationally-expensive computer simulations and/or analyses
- They provide a "model of a model" which can be used in place of the original computer simulation
- Surrogate modeling can be used to generate "smart objects" that can be used in place of the original analyses and integrated within any SBD infrastructure



# **Overview of Surrogate Modeling**

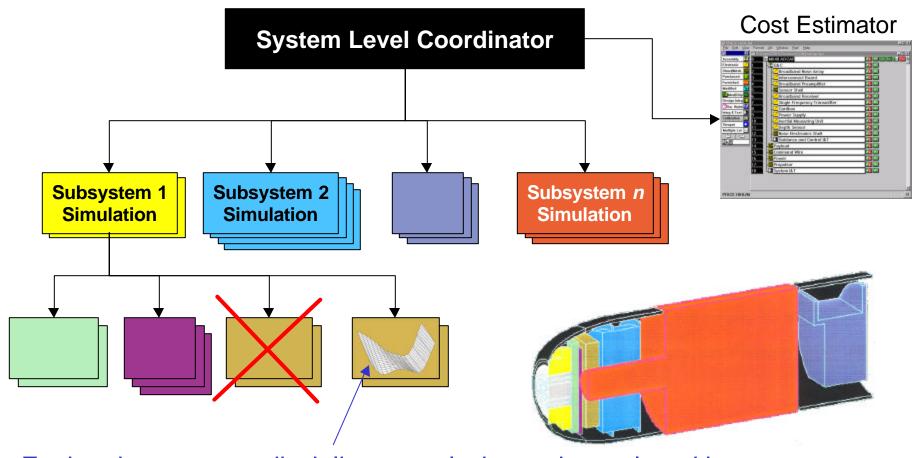
Generate simulation data using design of experiments capability

Use surrogate modeling capability to construct a "model of the model"





# **Surrogate Models in MDO**



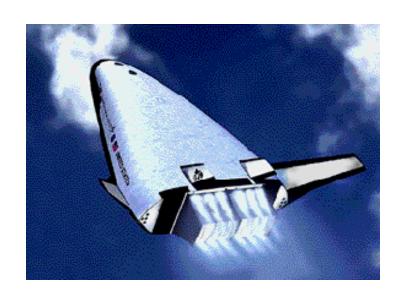
Each sub-system or disciplinary analysis can be replaced by a surrogate model and invoked by the higher-level coordinator



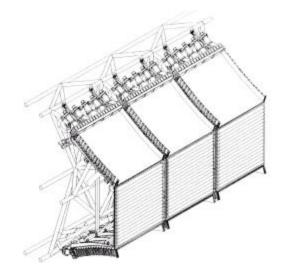


# **Application: Rocket Nozzle**

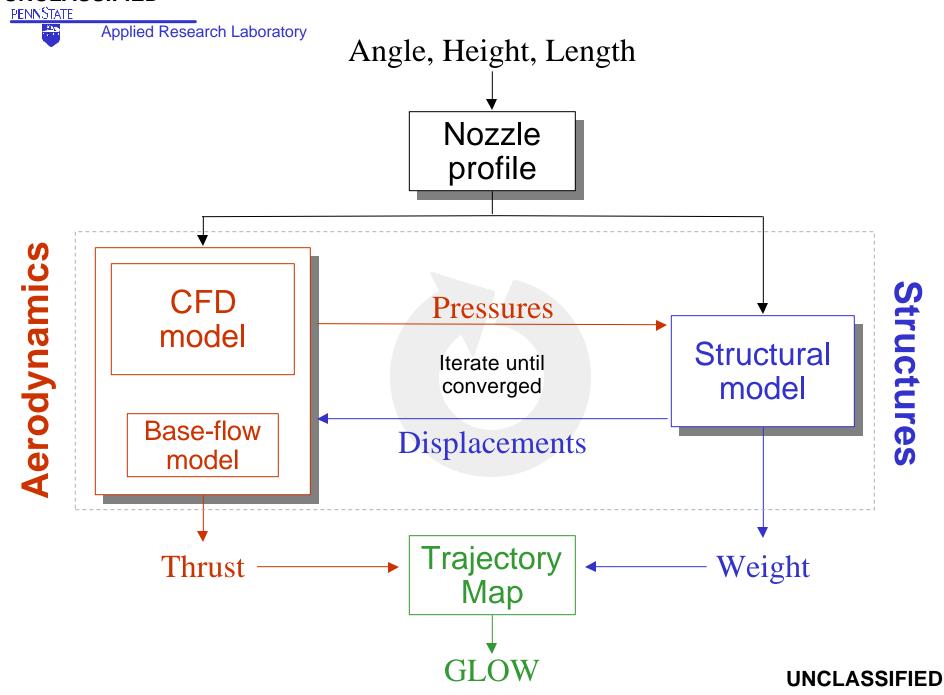
 Utilize surrogate models to facilitate multidisciplinary design and optimization of an aerospike rocket nozzle for the next generation shuttle



Venture Star RLV

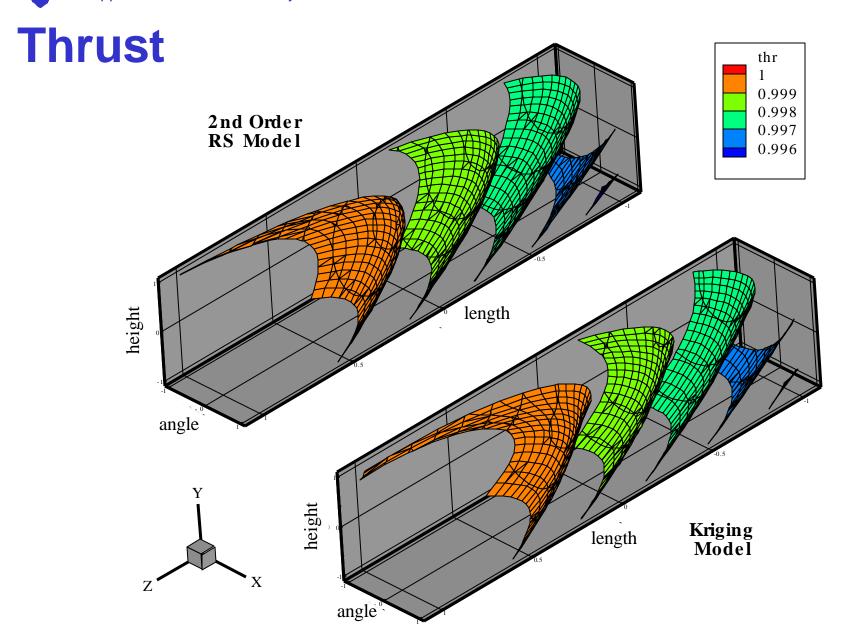


Aerospike Nozzle



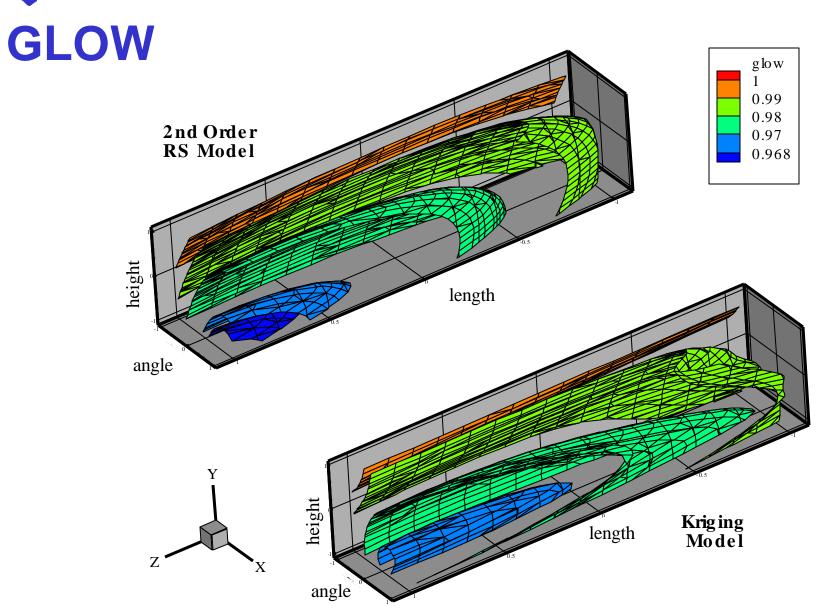
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# **Closing Remarks**

- MDO involves the coordination of multiple disciplinary analyses to realize more effective solutions during the design of complex systems
- Surrogate models can be used to address many of the computational challenges associated with MDO
- MDO formulations that incorporate uncertainty are currently being investigated



# For Further Reading

- McAllister, C. D. and Simpson, T. W. Multidisciplinary Robust Design Optimization of an Internal Combustion Engine, ASME Design Technical Conferences - Design Automation Conference (Diaz, A., ed.), Pittsburgh, PA, September 9-12, ASME, Paper No. DETC2001/DAC-21124.
- McAllister, C. D., Simpson, T. W. and Yukish, M. (2000) Goal Programming Applications in Multidisciplinary Design Optimization, 8th AIAA/NASA/USAF/ISSMO Symposium on Multidisciplinary Analysis and Optimization, Long Beach, CA, September 6-8, AIAA, AIAA-2000-4717.
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- Jin, R., Chen, W. and Simpson, T. W., "Comparative Studies of Metamodeling Techniques under Multiple Modeling Criteria," 8th AIAA/NASA/USAF/ISSMO Symposium on Multidisciplinary Analysis and Optimization, Long Beach, CA, AIAA, 2000, AIAA-2000-4801, to appear in Journal of Structural and Multidisciplinary Optimization.